



A logarithm is just a special way to ask a specific question
 "log base b of a is x"

$$\log_b a = x$$

THE QUESTION: What exponent is required to go from a base of b to reach a value of a

CONVERT BETWEEN EXPONENTIAL AND LOGARITHMIC FORM

$$\log_5 x = y \iff \left(\frac{1}{5}\right)^y = x$$

$$\log_9 x = y \iff 9^y = x$$

$$\log_6 x = y \iff 6^y = x$$

$$\log_{\frac{15}{16}} r = s \iff \left(\frac{15}{16}\right)^s = r$$

$$\log_{\frac{7}{4}} x = y \iff \left(\frac{7}{4}\right)^y = x$$

$$\log_4 x = y \iff 4^y = x$$

$$\log_4 x = y \iff 4^{-y} = \frac{1}{x}$$

The Logarithm Loop Trick

Always draw your loop counter-clockwise from the base!

$$\log_b a = x \iff b^x = a$$

EXPONENTIAL FORM

LOGARITHMIC FORM

base exponent = answer
 $\log_b a = x$ answer = exponent
 base goes to b
 exponent goes to a
 answer goes to x

CALCULATE THE FOLLOWING LOGARITHMS

$$\log_4 64 = y \iff 4^y = 64 \iff y = 3$$

$$\log_4 16 \iff 4^y = 16 \iff y = 2$$

$$\log_6 216 = y \iff 6^y = 216 \iff y = 3$$

$$\log_3 \frac{1}{243} \iff 3^y = \frac{1}{243} \iff y = -5$$

$\log_{343} 7$
 $343^x = 7$
 $7^3 = 7$
 $x = \frac{1}{3}$

$\log_{64} 4$
 $64^x = 4$
 $4^3 = 4$
 $x = \frac{1}{3}$

$\log_2 16$
 $2^x = 16$
 $x = 4$

$\log_6 \frac{1}{216}$
 $6^x = 216$
 $x = -3$

COMMON LOG
 OH NO!
 MY LOGARITHM HAS NO BASE
 ANYTIME THE BASE OF A LOGARITHM IS NOT WRITTEN, IT IS ASSUMED TO BE THE NUMBER 10

$\log 10 = \log_{10} 10 = 1$
 $\log \left(\frac{1}{10}\right) = \log_{10} \left(\frac{1}{10}\right) = -1$

NATURAL LOG
 write as \rightarrow $\ln x$
 $\log_e x$

basic Logs

Date _____ Period _____

Rewrite each equation in logarithmic form.

1) $5^2 = 25$

2) $9^2 = 81$

3) $5^{-2} = \frac{1}{25}$

4) $x^{11} = y$

5) $\left(\frac{1}{15}\right)^0 = 1$

6) $m^{-9} = n$

7) $16^0 = 1$

8) $12^2 = 144$

9) $18^2 = 324$

10) $y^x = z$

Evaluate each expression.

11) $\log_6 6$

12) $\log_3 -\frac{1}{27}$

13) $\log_2 16$

14) $\log_7 49$

15) $\log_5 125$

16) $\log_6 216$

17) $\log_7 -343$

18) $\log_2 8$

19) $\log_5 -25$

20) $\log_2 4$

PROPERTIES OF LOGARITHMS

PRODUCT PROPERTY

$$\log_b xy = \log_b x + \log_b y$$

QUOTIENT PROPERTY

$$\log_b \frac{x}{y} = \log_b x - \log_b y$$

POWER PROPERTY

$$\log_b x^y = y \log_b x$$

EXPANDING LOGARITHMS

$$\log_2 3x^4y = \log_2 3 + \log_2 x^4 + \log_2 y$$
$$\log_2 3 + 4 \log_2 x + \log_2 y$$

EXPANDING CONTINUED

$$\log \frac{a^2b}{c}$$
$$\log a^2b - \log c$$
$$\log a^2 + \log b - \log c$$
$$2 \log a + \log b - \log c$$

EXPANDING CONTINUED

$$\log_5 \frac{p}{q^2 r^3}$$

$$\log_5 p - \log_5 q^2 r^3$$

$$\log_5 p - 2 \log_5 q + 3 \log_5 r$$

EXPANDING CONTINUED

$$\log_7 (c^2 \sqrt[3]{a}) = \log_7 c^2 a^{\frac{1}{3}}$$

$$\log_7 c^2 + \log_7 a^{\frac{1}{3}}$$

$$2 \log_7 c + \frac{1}{3} \log_7 a$$

EXPANDING CONTINUED

$$\log_2 \sqrt{x \cdot y \cdot z}$$

$$\log_2 (xyz)^{\frac{1}{2}}$$

$$\frac{1}{2} \log_2 (xyz)$$

$$\frac{1}{2} (\log_2 x + \log_2 y + \log_2 z)$$

CONDENSING LOGARITHMS

$$\log_3 5 + 2 \log_3 x - 6 \log_3 z$$

$$\log_3 5 + \log_3 x^2 - \log_3 z^6$$

$$\log_3 5x^2 - \log_3 z^6$$

$$\log_3 \left(\frac{5x^2}{z^6} \right)$$

CONDENSING CONTINUED

$$2 \ln a - \ln b - 3 \ln c$$

$$\ln a^2 - \ln b - \ln c^3$$

$$\ln \frac{a^2}{b} - \ln c^3$$

$$\ln \frac{a^2}{bc^3}$$

CONDENSING CONTINUED

$$2(\log_4 6 - \log_4 3) + 0.5 \log_4 25$$

$$2 \log_4 \left(\frac{6}{3} \right) + \log_4 25^{\cdot 5}$$

$$\log_4 \left(\frac{6}{3} \right)^2 + \log_4 25^5$$

$$\log_4 \left(\left(\frac{6}{3} \right)^2 (25^5) \right)$$

Expand/Condense

Date _____ Period _____

Expand each logarithm.

1) $\log_8 (a^2 \cdot b)^3$

2) $\log_7 \frac{a^6}{b^4}$

3) $\log_9 (a^5 b^3)$

4) $\log_8 \left(\frac{x}{y^4} \right)^2$

5) $\log_7 (z \sqrt[3]{x \cdot y})$

Condense each expression to a single logarithm.

6) $4 \log_3 u - 2 \log_3 v$

7) $6 \log_5 c + \frac{\log_5 a}{2}$

8) $5 \log u - 6 \log v$

9) $16 \log_9 u + 4 \log_9 v$

10) $\frac{\log_3 u}{3} + \frac{\log_3 v}{3} + \frac{\log_3 w}{3}$

CHANGE OF BASE

$$b^{\log_b x} = x$$

Students draw anywhere on this slide!

Page 2 of 10 Interactive Slides

$$\log_b b^x = x$$

Students draw anywhere on this slide!

Page 3 of 10 Interactive Slides

EXAMPLES

$$10^{\log_{10} 6} = 6$$

Students draw anywhere on this slide!


Page 4 of 10 Interactive Slides



Students, draw anywhere on this slide!

$$\cdot \log_3 9x = \log_3 3^{2x} = 2x$$

Point to a reference slide



Students, draw anywhere on this slide!

$$\ln e^{\frac{x}{2}} \quad \frac{x}{2}$$


Point to a reference slide



Students, draw anywhere on this slide!

$$e^{\ln 3x} = 3x$$

Point to a reference slide



Students, draw anywhere on this slide!

CHANGE OF BASE FORMULA

$$\log_c a = \frac{\log a}{\log c}$$

Point to a reference slide

EVALUATE USING CHANGE OF BASE

$$\log_5 7 = \frac{\log 7}{\log 5} = 1.21$$



Students, draw anywhere on this slide!

Open the interactive slide

$$\log_2 5$$

$$\frac{\log 5}{\log 2} = 2.32$$



Students, draw anywhere on this slide!

Open the interactive slide

Change of Base

Date _____ Period _____

Use a calculator to approximate each to the nearest thousandth.

1) $\log_4 52$

2) $\log_4 23$

3) $\log_5 26$

4) $\log_6 6.16$

5) $\ln 8$

6) $\log_3 34$

7) $\log_2 5.5$

8) $\log_2 5.1$